smalljac in sage

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Computing L-series of hyperelliptic curves, Kedlaya-S



Fast computation of *L*-polynomials (or Frobenius charpolys) and Jacobian group structures for genus $g \le 2$ curves.

- Many performance enhancements.
- Prime bounds extended $(2^{40} \text{ in genus } 1, 2^{30} \text{ in genus } 2)$.
- Now handles all genus 2 curves.
- Quadratic number fields.
- Sato-Tate group identification (heuristic).

Fully integrated into (64-bit) sage.

Improves performance of existing sage functionality:

- E.aplist(B) typically 5x to 10x faster than using Pari (or Magma's TraceOfFrobenius), handles B up to 2⁴⁰.
- E.abelian_group() 5x to 20x faster.
- C.frobenius_polynomial() 10x to 20x faster for genus
 2 curves (and *much* faster than Magma's LPolynomial).

Adds new functionality to sage:

- aplists for curves over quadratic fields (e.g., $\mathbb{Q}(\sqrt{5})$)
- grouplists computes Jacobian group structures
- moments of *L*-poly coefficients
- histogram generation
- Sato-Tate group identification (as in FKRS 2012)

Demo

click here